



SOL 1.3

By writing KVL in input and output loops

$$V_1 - (i_1 + i_2) Z_1 = 0$$

$$V_1 = Z_1 i_1 + Z_1 i_2 \qquad \dots (1)$$

Similarly

$$V_{2} - i_{2}Z_{2} - (i_{1} + i_{2})Z_{1} = 0$$

$$V_{2} = Z_{1}i_{1} + (Z_{1} + Z_{2})i_{2} \qquad \dots (2)$$
From equation (1) and (2) Z-matrix is given as
$$Z = \begin{bmatrix} Z_{1} & Z_{1} \\ Z_{1} - Z_{1} + Z_{2} \end{bmatrix}$$
Hence (D) is correct option.

MCQ 1.4 In the figure given, for the initial capacitor voltage is zero. The switch is closed at t = 0. The final steady-state voltage across the capacitor is



SOL 1.4

1.4 In final steady state the capacitor will be completely charged and behaves as an open circuit



Steady state voltage across capacitor

$$v_c(\infty) = rac{20}{10+10}(10)$$

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	= 10	V	
	Hence (B) is correct option.		
MCQ 1.5	If \vec{E} is the electric intensi (A) \vec{E} (C) null vector	by, $\nabla (\nabla \times \vec{E})$ is equal to (B) $ \vec{E} $ (D) Zero	
SOL 1.5	We know that divergence $\nabla (\nabla \times \vec{\mathbf{E}}) = 0$ Hence (D) is correct optic	of the curl of any vector field is zero n.	
MCQ 1.6	2Q 1.6 A system with zero initial conditions has the closed loop transfer functor $T(s) = \frac{s^2 + 4}{(s+1)(s+4)}$		
	The system output is zero (A) 0.5 rad/sec (C) 2 rad/sec	at the frequency (B) 1 rad/sec (D) 4 rad/sec	
SOL 1.6	Closed loop transfer funct $T(s) = \frac{s^2 + 4}{(s+1)(s)}$ $T(j\omega) = \frac{(j\omega)^2}{(j\omega+1)(s)}$ If system output is zero $ T(j\omega) = \frac{ 4-1 }{ (j\omega+1) }$ $4 - \omega^2 = 0$ $\omega^2 = 4$ $\Rightarrow \omega = 2 \text{ rad/sec}$ Hence (C) is correct option	ton of the given system is, $\overline{\mathbf{J}_{4}^{(4)}} \mathbf{a} \mathbf{f} \mathbf{e}$ $\overline{\mathbf{J}_{4}^{(4)}} \mathbf{h} \mathbf{e} \mathbf{p}$ $\overline{\mathbf{h}} \mathbf{e} \mathbf{p}$ $\frac{\omega^{2}}{j\omega + 4} = 0$	

MCQ 1.7 Figure shows the root locus plot (location of poles not given) of a third order system whose open loop transfer function is



(A)
$$\frac{K}{s^3}$$
 (B) $\frac{K}{s^2(s+1)}$
(C) $\frac{K}{s(s^2+1)}$ (D) $\frac{K}{s(s^2-1)}$

SOL 1.7

1.7 From the given plot we can see that centroid C (point of intersection) where asymptotes intersect on real axis) is 0 So for option (a)

For option (a)

$$G(s) = \frac{K}{s^3}$$
Centroid = $\frac{\sum \text{Poles} - \sum \text{Zeros}}{n-m} = \frac{0-0}{3-0} = 0$

Hence (A) is correct option.

MCQ 1.8 The gain margin of a unity feed back control system with the open loop transfer function

$$G(s) = \frac{(s+1)}{s^2} \text{ is } \tag{B) } \frac{1}{\sqrt{2}}$$
(A) 0
(B) $\frac{1}{\sqrt{2}}$
(C) $\sqrt{2}$

SOL 1.8 Open loop transfer function is. $G(s) = \frac{(s+1)}{s^2}$

$$G(j\omega) = \frac{j\omega + 1}{-\omega^2}$$

Phase crossover frequency can be calculated as.

$$egin{aligned} & \angle G(j\omega_p) = -\ 180^\circ \ an^{-1}(\omega_p) = -\ 180^\circ \ \omega_p = 0 \end{aligned}$$

Gain margin of the system is.

$$\mathrm{G.M} = rac{1}{\left| \, G(j\omega_p) \,
ight|} = rac{1}{rac{\sqrt{\omega_p^2 + 1}}{\omega_n^2}}$$

$$G.M = \frac{\omega_p^2}{\sqrt{\omega_p^2 + 1}} = 0$$

Hence (A) is correct option.

- **MCQ 1.9** In the matrix equation $P\mathbf{x} = \mathbf{q}$, which of the following is a necessary condition for the existence of at least on solution for the unknown vector \mathbf{x}
 - (A) Augmented matrix $[P\mathbf{q}]$ must have the same rank as matrix P
 - (B) Vector **q** must have only non-zero elements

Page 5 **GATE EE 2005** www.gatehelp.com (C) Matrix P must be singular (D) Matrix P must be square **SOL 1.9** The Correct option is (D). For two random events conditional probability is given by probability $(P \cap Q)$ = probability (P) probability (Q)probability $(Q) = \frac{\text{probability}(P \cap Q)}{\text{probability}(P)} \le 1$ so probability $(P \cap Q) \leq \text{probability}(P)$ If P and Q are two random events, then the following is TRUE **MCQ 1.10** (A) Independence of P and Q implies that probability $(P \cap Q) = 0$ (B) Probability $(P \cup Q) \ge$ Probability (P) + Probability (Q) (C) If P and Q are mutually exclusive, then they must be independent (D) Probability $(P \cap Q) \leq$ Probability (P) **SOL 1.10** Option (D) is correct. for two random events conditional probability is given by $\begin{array}{l} \operatorname{probability}\left(P \cap \ Q\right) = \operatorname{probability}\left(P\right) \operatorname{probability}\left(Q\right) \\ \operatorname{probability}\left(Q\right) = \frac{\operatorname{probability}\left(P \cap \ Q\right)}{\operatorname{probability}\left(P\right)} \leq 1 \end{array}$ probability $(P \cap Q) \leq \text{probability}(P)$ \mathbf{SO} If $S = \int_{1}^{\infty} x^{-3} dx$, then S has the value **MCQ 1.11** (A) $-\frac{1}{3}$ (B) $\frac{1}{4}$ (C) $\frac{1}{2}$ (D) 1 SOL 1.11 Hence (C) is correct option $S = \int_{0}^{\infty} x^{-3} dx$ $=\left[\frac{x^{-2}}{-2}\right]_{1}^{\infty}$ $=\frac{1}{2}$

MCQ 1.12 The solution of the first order differential equation $x'(t) = -3x(t), x(0) = x_0$ is

(A)
$$x(t) = x_0 e^{-3t}$$

(B) $x(t) = x_0 e^{-3}$
(C) $x(t) = x_0 e^{-1/3}$
(D) $x(t) = x_0 e^{-1}$

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SOL 1.12	Hence (A) is correct option. We have $\dot{x}(t) = -3x(t)$ or $\dot{x}(t) + 3x(t) = 0$ A.E. $D+3 = 0$ Thus solution is $x(t) = C_1 e^{-3t}$ From $x(0) = x_0$ we get $C_1 = x_0$ Thus $x(t) = x_0 e^{-3t}$	
MCQ 1.13	The equivalent circuit of a transformer has reactance X_M . Their magnitudes satisfy	leakage reactances X_1, X_2 and magnetizing
	(A) $X_1 >> X_2 >> X_M$	(B) $X_1 << X_2 << X_M$
	(C) $X_1 \approx X_2 >> X_M$	(D) $X_1 \approx X_2^{\prime} \ll X_M$
SOL 1.13	The Correct option is (D). The leakage reactances X_1 , and X_2' are higher than X_1 , and X_2' $X_1 \approx X_2' << X_m$	e equal and magnetizing reactance X_m is
MCQ 1.14	Which three-phase connection can be us difference of 30° between its output and (A) Star-Star (C) Delta-Delta	sed in a transformer to introduce a phase corresponding input line voltages(B) Star-Delta(D) Delta-Zigzag
SOL 1.14	The Correct option is (B). Three phase star delta connection of tran between output and input line voltage.	nsformer induces a phase difference of 30°
MCQ 1.15	On the torque/speed curve of the induct of operation are marked as W, X, Y as operation at a slip greater than 1 ? Torque $\begin{array}{c} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$	ion motor shown in the figure four points nd Z. Which one of them represents the
	(A) W	(B) X
SOI 1 45	(U) Y The Correct option is (Λ)	(D) Z



When the speed of the motor is in forward direction then slip varies from 0 to 1 but when speed of motor is in reverse direction or negative then slip is greater than 1. So at point W slip is greater than 1.

MCQ 1.16 For an induction motor, operation at a slip s, the ration of gross power output to air gap power is equal to

(A)
$$(1-s)^2$$

(B) $(1-s)$
(D) $(1-\sqrt{s})$

SOL 1.16The Correct option is (B).
For an induction motor the ratio of gross power output to air-gap is equal to (1 - s)
SoSo $\frac{\text{gross power}}{\text{airgap power}} = (1 - s)$

MCQ 1.17The p.u. parameter for a 500 MVA machine on its own base are:
inertia, M = 20 p.u.; reactance, X = 2 p.u.
The p.u. values of inertia and reactance on 100 MVA common base, respectively,
are
(A) 4, 0.4
(B) 100, 10
(C) 4, 10(B) 100, 10
(D) 100, 0.4

SOL 1.17 The Correct option is (D).

Given that pu parameters of 500 MVA machine are as following

$$M = 20$$
 pu, $X = 2$ pu

Now value of M and X at 100 MVA base are for inertia (M)

$$(\mathrm{pu})_{\mathrm{new}} = (\mathrm{pu})_{\mathrm{old}} \times rac{\mathrm{old} \ \mathrm{MVA}}{\mathrm{new} \ \mathrm{MVA}}$$
 $(M_{\mathrm{pu}})_{\mathrm{new}} = (M_{\mathrm{Pu}})_{\mathrm{old}} \times rac{500}{100}$
 $= 20 \times rac{5}{1} = 100 \ \mathrm{pu}$

and for reactance (X)

$$(\mathrm{pu})_{\mathrm{new}} = (\mathrm{pu})_{\mathrm{old}} \times \frac{\mathrm{new} \,\mathrm{MVA}}{\mathrm{old} \,\mathrm{MVA}}$$

 $(X_{\mathrm{pu}})_{\mathrm{new}} = (X_{\mathrm{pu}})_{\mathrm{old}} \times \frac{100}{500}$

	$(X_{ m Pu})_{ m new} = 2 imes rac{1}{5} = 0.4$;	pu
MCQ 1.18	An 800 kV transmission line has a m operated at 400 kV with the series re- transfer capacity is approximately (A) P (C) $P/2$	maximum power transfer capacity of P . If it is eactance unchanged, the new maximum power (B) $2P$ (D) $P/4$
SOL 1.18	The Correct option is (D). 800 kV has Power transfer capacity = At 400 kV Power transfer capacity = We know Power transfer capacity $P = \frac{EV}{X} \sin \delta$ $P \propto V^2$	= P = ?
	$P \propto V^{-}$ So if V is half than Power transfer c	apacity is $\frac{1}{2}$ of previous value
MCQ 1.19	The insulation strength of an EHV t (A) load power factor (C) harmonics	 ransmission line is mainly governed by (B) switching over-voltages (D) corona
SOL 1.19	The Correct option is (B). In EHV lines the insulation streng voltages.	G h of line is governed by the switching over
MCQ 1.20	 High Voltage DC (HVDC) transmiss (A) bulk power transmission over ver (C) inter-connecting two systems with (C) eliminating reactive power require (D) minimizing harmonics at the context of the context	ion is mainly used for ry long distances th same nominal frequency rement in the operation overter stations
SOL 1.20	The Correct option is (A). For bulk power transmission over ver used.	y long distance HVDC transmission preferably
MCQ 1.21	The Q-meter works on the principle (A) mutual inductance (C) series resonance	of (B) self inductance (D) parallel resonance
SOL 1.21	The Correct option is (C). Q-meter works on the principle of se	ries resonance.



- **MCQ 1.22** $V_1 = 2$ V and AC voltage source $V_2(t) = 3\sin(4t)$ V. The meter reads
- SOL 1.22
- Assume that D_1 and D_2 in figure are ideal diodes. The value of current is **MCQ 1.23**



(A) 0 mA	(B) 0.5 mA
(C) 1 mA	(D) 2 mA

SOL 1.23 The Correct option is (A).

> From the circuit we can observe that Diode D_1 must be in forward bias (since current is flowing through diode).

Let assume that D_2 is in reverse bias, so equivalent circuit is.





MCQ 1.24 The 8085 assembly language instruction that stores the content of H and L register into the memory locations $2050_{\rm H}$ and $2051_{\rm H}$, respectively is

(A) SPHL $2050_{\rm H}$	(B) SPHL $2051_{\rm H}$
(C) SHLD $2050_{\rm H}$	(D) STAX $2050_{\rm H}$

- SOL 1.24The Correct option is (C).
SHLD transfers contain of HL pair to memory location.
SHLD $2050 \Rightarrow L \rightarrow M[2050H]$
H $\rightarrow M[2051H]$ Here M
- **MCQ 1.25** Assume that the N-channel MOSFET shown in the figure is ideal, and that its threshold voltage is +1.0 V the voltage V_{ab} between nodes a and b is



(A) 5 V	(B) 2 V
(C) 1 V	(D) 0 V

SOL 1.25 The Correct option is (D). This is a N-channel MOSFET with $V_{GS} = 2 V$ $V_{TH} = +1 V$

$$V_{DS(\text{sat})} \equiv V_{GS} - V_{TH}$$

 $V_{DS(\text{sat})} = 2 - 1 = 1$ V

Due to 10 V source $V_{DS} > V_{DS(sat)}$ so the NMOS goes in saturation, channel

conductivity is high and a high current flows through drain to source and it acts as a short circuit.

So,
$$V_{ab} = 0$$

MCQ 1.26 The digital circuit shown in the figure works as



(A) JK flip-flop

- (B) Clocked RS flip-flop
- (C) T flip-flop (D) Ring counter
- **SOL 1.26** The Correct option is (C). Let the present state is Q(t), so input to D-flip flop is given by, $D = Q(t) \oplus X$ Next state can be obtained as, Q(t+1) = D

and

$$Q(t+1) = Q(t) \oplus X$$

$$Q(t+1) = Q(t) \overline{X} + \overline{Q}(t) X$$

$$Q(t+1) = \overline{Q}(t), \quad \text{if } X = 1$$

$$Q(t+1) = Q(t), \quad \text{if } X = 0$$

So the circuit behaves as a T flip flop.

- **MCQ 1.27** A digital-to-analog converter with a full-scale output voltage of 3.5 V has a resolution close to 14 mV. Its bit size is
 - (A) 4 (B) 8 (C) 16 (D) 32
- **SOL 1.27** The Correct option is (B).

Resolution of n-bit DAC = $\frac{V_{fs}}{2^n - 1}$

So

$$14 mv = \frac{3.5 V}{2^{n} - 1}$$

$$2^{n} - 1 = \frac{3.5}{14 \times 10^{-3}}$$

$$2^{n} - 1 = 250$$

$$2^{n} = 251$$

$$n = 8 \text{ bit}$$

MCQ 1.28 The conduction loss versus device current characteristic of a power MOSFET is best approximated by

(A) a parabola

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	(B) a straight line
	(C) a rectangular hyperbola
	(D) an exponentially decaying function
SOL 1.28	The Correct option is (A). The conduction loss v/s MOSFET current characteristics of a power MOSFET is best approximated by a parabola.
MCQ 1.29	A three-phase diode bridge rectifier is fed from a 400 V RMS, 50 Hz, three-phase AC source. If the load is purely resistive, then peak instantaneous output voltage is equal to
	(A) 400 V (B) $400\sqrt{2}$ V
	(C) $400\sqrt{\frac{2}{3}}$ V (D) $\frac{400}{\sqrt{3}}$ V
SOL 1.29	The Correct option is (B).
	In a 3- ϕ bridge rectifier $V_{-} = 400 V_{-} f_{-} = 50 H_{Z}$
	This is purely resistive then $V_{\rm rms} = 400$ V, $J = 50$ Hz
	instantaneous voltage $V_0 = \sqrt{2} V_{\rm rms} = 400\sqrt{2}$ V
MCQ 1.30	The output voltage waveform of a three-phase square-wave inverter contains (A) only even harmonics (B) both odd and even harmonic
	(C) only odd harmonics (D) only triple harmonics
SOL 1.30	The Correct option is (C).
	A 3- ϕ square wave (symmetrical) inverter contains only odd harmonics.

Q.31 - 80 Carry Two Marks Each

MCQ 1.31 The RL circuit of the figure is fed from a constant magnitude, variable frequency sinusoidal voltage source V_{in} . At 100 Hz, the R and L elements each have a voltage drop μ_{RMS} . If the frequency of the source is changed to 50 Hz, then new voltage drop across R is



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SOL 1.31 The Correct option is (C).
At
$$f_i = 100$$
 Hz, voltage drop across R and L is μ_{RMS}
 $\mu_{\text{RMS}} = \left| \frac{V_{in} \cdot R}{R + j\omega_1 L} \right| = \left| \frac{V_{in}(j\omega_1 L)}{R + j\omega_1 L} \right|$
So, $R = \omega_1 L$
at $f_2 = 50$ Hz, voltage drop across R
 $\mu'_{\text{RMS}} = \left| \frac{R + j\omega_2 L}{R + j\omega_2 L} \right|$
 $\frac{\mu_{\text{RMS}}}{\mu'_{\text{RMS}}} = \left| \frac{R + j\omega_2 L}{R^2 + \omega_1^2 L^2} \right|$
 $= \sqrt{\frac{R^2 + \omega_2^2 L^2}{\omega_1^2 L^2 + \omega_1^2 L^2}}, R = \omega_1 L$
 $= \sqrt{\frac{\omega_1^2 + \omega_2^2}{2\omega_1^2}} = \sqrt{\frac{f_1^2 + f_2^2}{2f_1^2}}$
 $= \sqrt{\frac{(100)^2 + (50)^2}{2(100)^2}} = \sqrt{\frac{5}{8}}$
 $\mu'_{\text{RMS}} = \sqrt{\frac{8}{5}} \mu_{\text{RMS}}$

MCQ 1.32 For the three-phase circuit shown in the figure the ratio of the currents $I_R: I_Y: I_B$ is given by



SOL 1.32 The Correct option is (A). In the circuit

 \therefore so,

$$egin{aligned} \overline{I}_B &= I_R otooldsymbol{\&} 0^\circ + I_y otooldsymbol{\&} 120^\circ \ I_B^2 &= I_R^2 + I_y^2 + 2I_R I_y \cos\left(rac{120^\circ}{2}
ight) \ I_B^2 &= I_R^2 + I_y^2 + I_R I_y \ I_R &= I_y \ I_B^2 &= I_R^2 + I_R^2 + I_R^2 = 3I_R^2 \end{aligned}$$

 $I_B = \sqrt{3} I_R = \sqrt{3} I_y$ $I_R: I_y: I_B = 1:1:\sqrt{3}$





MCQ 1.34 The circuit shown in the figure is in steady state, when the switch is closed at t = 0. Assuming that the inductance is ideal, the current through the inductor at $t = 0^+$ equals







Switch was opened before t = 0, so current in inductor for t < 0



Inductor current does not change simultaneously so at t = 0 when switch is closed current remains same $i_L(0^+) = i_L(0^-) = 1$ A

(B) 0.5 A

(D) 2 A

MCQ 1.35 The charge distribution in a metal-dielectric-semiconductor specimen is shown in the figure. The negative charge density decreases linearly in the semiconductor as shown. The electric field distribution is as shown in



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SOL 1.35 The Correct option is (A).
Electric field inside a conductor (metal) is zero. In dielectric charge distribution os constant so electric field remains constant from x_1 to x_2. In semiconductor electric field varies linearly with charge density.
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MCQ 1.36 In the given figure, the Thevenin's equivalent pair (voltage, impedance), as seen at the terminals P-Q, is given by



Thevenin voltage:

SOL 1.36



(C) |K| < 1 (D) K < -1

SOL 1.37

1.37 Characteristic equation for the given system 1 + C(x) + W(x) = 0

$$1 + G(s) H(s) = 0$$

$$1 + K \frac{(1-s)}{(1+s)} = 0$$

$$(1+s) + K(1-s) = 0$$

$$s(1-K) + (1+K) = 0$$

For the system to be stable, coefficient of characteristic equation should be of same sign.

$$1 - K > 0, K + 1 > 0$$

 $K < 1, K > -1$
 $-1 < K < 1$
 $|K| < 1$
ence (C) is correct option

Hence (C) is correct option

MCQ 1.38 When subject to a unit step input, the closed loop control system shown in the figure will have a steady state error of



Hence (C) is correct option.

MCQ 1.39 In the G(s) H(s)-plane, the Nyquist plot of the loop transfer function $G(s) H(s) = \frac{\pi e^{-0.25s}}{s}$

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SOL 1.38

SOL 1.39

When it passes through negative real axis at that point phase angle is -180° . $\angle G(j\omega) H(j\omega) = -180^{\circ}$ So

$$-0.25j\omega - \frac{\pi}{2} = -\pi$$
$$-0.25j\omega = -\frac{\pi}{2}$$
$$j0.25\omega = \frac{\pi}{2}$$
$$j\omega = \frac{\pi}{2 \times 0.25}$$
$$s = j\omega = 2\pi$$

Put $s = 2\pi$ in given open loop transfer function we get

$$G(s) H(s) \Big|_{s=2\pi} = \frac{\pi e^{-0.25 \times 2\pi}}{2\pi} = -0.5$$

So it passes through (-0.5, j0)Hence (B) is correct option.

MCQ 1.40 If the compensated system shown in the figure has a phase margin of 60° at the crossover frequency of 1 rad/sec, then value of the gain K is



SOL 1.40

Open loop transfer function of the system is given by.

$$G(s) H(s) = (K+0.366s) \left[\frac{1}{s(s+1)} \right]$$
$$G(j\omega) H(j\omega) = \frac{K+j0.366\omega}{j\omega(j\omega+1)}$$

Phase margin of the system is given as

 $\phi_{\rm PM} = 60^{\circ} = 180^{\circ} + \angle G(j\omega_a) H(j\omega_a)$

Where $\omega_q \rightarrow \text{gain cross over frequency} = 1 \text{ rad/sec}$ So,

$$60^{\circ} = 180^{\circ} + \tan^{-1} \left(\frac{0.366 \omega_g}{K} \right) - 90^{\circ} - \tan^{-1} (\omega_g)$$

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$$= 90^{\circ} + \tan^{-1} \left(\frac{0.366}{K} \right) - \tan^{-1}(1)$$
$$= 90^{\circ} - 45^{\circ} + \tan^{-1} \left(\frac{0.366}{K} \right)$$
$$15^{\circ} = \tan^{-1} \left(\frac{0.366}{K} \right)$$
$$\frac{0.366}{K} = \tan 15^{\circ}$$
$$K = \frac{0.366}{0.267} = 1.366$$

Hence (C) is correct option.

MCQ 1.41 For the matrix $p = \begin{bmatrix} 3 & -2 & 2 \\ 0 & -2 & 1 \\ 0 & 0 & 1 \end{bmatrix}$, one of the eigen values is equal to -2

Which of the following is an eigen vector ?

(A)
$$\begin{bmatrix} 3\\ -2\\ 1 \end{bmatrix}$$

(C) $\begin{bmatrix} 1\\ -2\\ 3 \end{bmatrix}$
(C) $\begin{bmatrix} 1\\ -2\\ 3 \end{bmatrix}$
(C) $\begin{bmatrix} 1\\ -2\\ 3 \end{bmatrix}$
(D) $\begin{bmatrix} -3\\ 2\\ -1 \end{bmatrix}$
(E) $\begin{bmatrix} -3\\ -2\\ -2 \end{bmatrix}$
(E) $\begin{bmatrix}$

SOL 1.41Hence (D) is correct option.For eigen value $\lambda = -2$

$$\begin{bmatrix} 3 - (-2) & -2 & 2 \\ 0 & -2 - (-2) & 1 \\ 0 & 0 & 1 - (-2) \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$
$$\begin{bmatrix} 5 & -2 & 2 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$
$$5x_1 - 2x_2 + x_3 = 0$$

Only option (D) satisfies this equation

MCQ 1.42 If
$$R = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 1 & -1 \\ 2 & 3 & 2 \end{bmatrix}$$
, then top row of R^{-1} is
(A) $\begin{bmatrix} 5 & 6 & 4 \end{bmatrix}$ (B) $\begin{bmatrix} 5 & -3 & 1 \end{bmatrix}$
(C) $\begin{bmatrix} 2 & 0 & -1 \end{bmatrix}$ (D) $\begin{bmatrix} 2 & -1 & 1/2 \end{bmatrix}$

SOL 1.42 Hence (B) is correct option.

$$C_{11} = 2 - (-3) = 5$$

$$C_{11} = -(0 - (-3)) = -3$$

$$C_{21} = (-(0 - (-3)) = 1$$

$$R = (1) C_{11} + 2C_{31} + 2C_{31}$$

$$= 5 - 6 + 2 = 1$$
MCQ 1.43 A fair coin is tossed three times in succession. If the first toss produces a head, then the probability of getting exactly two heads in three tosses is
(A) $\frac{1}{8}$
(B) $\frac{1}{2}$
(C) $\frac{3}{6}$
(D) $\frac{3}{4}$
Sol. 1.43 If the toss produces head, then for exactly two head in three tosses three tosses there must produce one head in next two tosses. The probability of one head in two tosses will be 1/2. Hence (B) is correct option.
MCQ 1.44 For the function $f(x) = x^2 e^{-x}$, the maximum occurs when x is equal to
(A) 2
(B) 1
(C) 0
(B) 1
(D) -1
Sol 1.44 Hence (A) is correct option.
MCQ 1.45 For the scalar field $u = \frac{x^2}{2} + \frac{y^2}{3}$, magnitude of the gradient at the point (1, 3) is
(A) $\sqrt{\frac{13}{9}}$
(C) $\sqrt{5}$
(D) $\frac{9}{2}$
Sol 1.45 Hence (C) is correct option.
 $\nabla u = \left(i \frac{\partial}{\partial x} + i \frac{\partial}{\partial y}\right)u$
 $= i \frac{\partial}{\partial x} u + i \frac{\partial}{\partial u}$

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$$= x\hat{\mathbf{i}} + \frac{2}{3}y\hat{\mathbf{j}}$$

At (1, 3) magnitude is $|\nabla u| = \sqrt{x^2 + (\frac{2}{3}y)^2}$
$$= \sqrt{1+4}$$
$$= \sqrt{5}$$

MCQ 1.46 For the equation x''(t) + 3x'(t) + 2x(t) = 5, the solution x(t) approaches which of the following values as $t \to \infty$?

(A) 0	(B) $\frac{5}{2}$
(C) 5	(D) 10

SOL 1.46 Hence (B) is correct option. $\frac{d^2x}{dt^2} + \frac{3dx}{dt} + 2x(t) = 5$

Taking laplace transform on both sides of above equation.

$$s^{2}X(s) + 3sX(s) + 2X(s) = \frac{5}{s}$$

$$X(s) = \frac{5}{s(s^{2} + 3s + 2)}$$
From final value theorem
$$\lim_{t \to \infty} x(t) = \lim_{s \to 0} X(s) \operatorname{eq}_{s \to 0}$$

$$= \lim_{s \to 0} s \frac{5}{s(s^{2} + 3s + 2)}$$

$$= \frac{5}{2}$$

MCQ 1.47 The Laplace transform of a function f(t) is $F(s) = \frac{5s^2 + 23s + 6}{s(s^2 + 2s + 2)}$ as $t \to \infty$, f(t) approaches (A) 3 (B) 5 (C) $\frac{17}{2}$ (D) ∞

SOL 1.47 The Correct option is (A).
By final value theorem
$$\lim_{t \to \infty} f(t) = \lim_{s \to 0} s F(s)$$
$$= \lim_{s \to 0} s \frac{(5s^2 + 23s + 6)}{s(s^2 + 2s + 2)}$$

$$= \frac{6}{2} = 3$$
MCQ 1.48 The Fourier series for the function $f(x) = \sin^2 x$ is
(A) $\sin x + \sin 2x$ (B) $1 - \cos 2x$

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(C)
$$\sin 2x + \cos 2x$$

(D) $0.5 - 0.5 \cos 2x$
SOL 1.48 The Correct option is (D).
 $f(x) = \sin^2 x$
 $= \frac{1 - \cos 2x}{2}$
 $= 0.5 - 0.5 \cos 2x$
 $f(x) = A_0 + \sum_{n=1}^{\infty} a_n \cos n\omega_0 x + b_n \sin n\omega_0 x$
 $f(x) = \sin^2 x$ is an even function so $b_n = 0$
 $A_0 = 0.5$
 $a_n = \begin{cases} -0.5, n = 1 \\ 0, \text{ otherwise} \end{cases}$
 $\omega_0 = \frac{2\pi}{T_0} = \frac{2\pi}{T} = 2$
MCQ 1.49 If $u(t)$ is the unit step and $\delta(t)$ is the unit impulse function, the inverse z-transform of $F(z) = \frac{1}{z+1}$ for $k > 0$ is
(A) $(-1)^k \delta(k)$
(C) $(-1)^k u(k)$
SOL 1.49 The Correct option is (B).
Z-transform $F(z) = \frac{1}{z+1}$
 $= 1 - \frac{z}{z+1} = 1 - \frac{1}{1+z^{-1}}$
so, $f(k) = \delta(k) - (-1)^k$
Thus $(-1)^k \stackrel{\checkmark}{\longleftarrow} \frac{1}{1+z^{-1}}$

MCQ 1.50 Two magnetic poles revolve around a stationary armature carrying two coil $(c_1 - c_1', c_2 - c_2')$ as shown in the figure. Consider the instant when the poles are in a position as shown. Identify the correct statement regarding the polarity of the induced emf at this instant in coil sides c_1 and c_2 .





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2. ϕ and ω only

R. Developed power (P)				3. ϕ and I_a only
				4. I_a and ω only
				5. I_a only
Code	es:			
	Р	\mathbf{Q}	R	
(A)	3	3	1	
(B)	2	5	4	
(C)	3	5	4	
(D)	2	3	1	

SOL 1.52 The Correct option is (D). In DC motor

Q. Developed torque (T)

or

$$E = PN\phi\left(\frac{Z}{A}\right)$$
$$E = K\phi\omega_n$$

So

Armature emf E depends upon ϕ and ω only.

and torque developed depends upon

$$T = \frac{PZ\phi I_a}{2\pi A}$$

So, torque(T) is depends of ϕ and I_a and developed power(P) is depend of flux ϕ , speed ω and armature current I_a .

- **MCQ 1.53** In relation to the synchronous machines, which on of the following statements is false ?
 - (A) In salient pole machines, the direct-axis synchronous reactance is greater than the quadrature-axis synchronous reactance.
 - (B) The damper bars help the synchronous motor self start.
 - (C) Short circuit ratio is the ratio of the field current required to produces the rated voltage on open circuit to the rated armature current.
 - (D) The V-cure of a synchronous motor represents the variation in the armature current with field excitation, at a given output power.
- **SOL 1.53** The Correct option is (C).

In synchronous machine, when the armature terminal are shorted the field current should first be decreased to zero before started the alternator.

In open circuit the synchronous machine runs at rated synchronous speed. The field current is gradually increased in steps.

The short circuit ratio is the ratio of field current required to produced the rated voltage on open to the rated armature current.

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MCQ 1.54	Under no load condition, if the from the rated voltage to half (A) the speed decreases and the (B) both the speed and the stator of (C) the speed and the stator of (D) there is negligible change	the applied voltage to an in the rated value, the stator current increase ator current decreases current remain practically in the speed but the state	induction motor is reduced s constant or current decreases
SOL 1.54	The Correct option is ()		
MCQ 1.55	A three-phase cage induction r the rated voltage. If the startin the full load slip is 4%, then ra- torque is approximately equal (A) 0.24 (C) 2.40	notor is started by direct- ig current drawn is 6 time atio of the starting develo to (B) 1.44 (D) 6.00	on-line (DOL) switching at es the full load current, and oped torque to the full load
SOL 1.55	The Correct option is (B). Given a three-phase cage indu- rated voltage. The starting cur- Full load slip = 4% So $\left(\frac{T_{\rm St}}{T_{\rm Fl}}\right) = \left(\frac{I_{\rm St}}{I_{\rm Fl}}\right)^2 \times$ $= (6)^2 \times$	ction motor is started by rrent drawn is 6 time the a t e $\langle S_{F1}$ 0.04 = 1.44	direct on line switching at full load current.
MCQ 1.56	In a single phase induction more resistance rotor is to achieve (A) low starting torque (C) high efficiency	otor driving a fan load, th (B) quick acce (D) reduced si	ne reason for having a high eleration ze
SOL 1.56	Given single-phase induction r So $E_b = V - I_a$ $\therefore \qquad P_{\text{mech}} = E_a I_a$ $\tau = \frac{P_{\text{mech}}}{\omega_m}$ From equation (1) and (2) th	notor driving a fan load, R_a ne high resistance of roto	the resistance rotor is high (1) (2) or then the motor achieves
	quick acceleration and torque Hence (B) is correct option.	of starting is increase.	
MCQ 1.57	Determine the correctness of reason[R] Assertion [A] : Under V/f co	ontrol of induction mote	wing assertion[A] and the or, the maximum value of

the developed torque remains constant over a wide range of speed in the sub-

-

synchronous region.

Reason [R] : The magnetic flux is maintained almost constant at the rated value by keeping the ratio V/f constant over the considered speed range.

- (A) Both [A] and [R] are true and [R] is the correct reason for [A]
- (B) Both [A] and [R] are true and but [R] is not the correct reason for [A]
- (C) Both [A] and [R] are false
- (D) [A] is true but [R] is false
- **SOL 1.57** The Correct option is (A).

Given V/f control of induction motor, the maximum developed torque remains same

we have,

$$E = 4.44 K_{w_1} \mathrm{f} \mathrm{\phi} \mathrm{T}_1$$

If the stator voltage drop is neglected the terminal voltage E_1 . To avoid saturation and to minimize losses motor is operated at rated airgap flux by varying terminal voltage with frequency. So as to maintain (V/f) ratio constant at the rated value, the magnetic flux is maintained almost constant at the rated value which keeps maximum torque constant.

MCQ 1.58 The parameters of a transposed overhead transmission line are given as :

Self reactance $X_S = 0.4\Omega/\text{km}$ and Mutual reactance $X_m = 0.1\Omega/\text{km}$ The positive sequence reactance X_1 and zero sequence reactance X_0 , respectively in Ω/km are (A) 0.3, 0.2 (B) 0.5, 0.2

(C) 0.5, 0.6 (D)	0.3,	0.	6
----	---------------	---	---	------	----	---

SOL 1.58 The Correct option is (D).

Parameters of transposed overhead transmission line

$$X_S = 0.4 \,\Omega/\mathrm{km}, \ X_m = 0.1 \,\Omega/\mathrm{km}$$

- +ve sequence reactance $X_1 = ?$
- Zero sequence reactance $X_0 = ?$

We know for transposed overhead transmission line.

- +ve sequence component $X_1 = X_S X_m$ = 0.4 - 0.1 = 0.3 Ω /km Zero sequence component $X_0 = X_S + 2X_m$ = 0.4 + 2 (0.1) = 0.6 Ω /km
- MCQ 1.59 At an industrial sub-station with a 4 MW load, a capacitor of 2 MVAR is installed to maintain the load power factor at 0.97 lagging. If the capacitor goes out of service, the load power factor becomes

(A) 0.85	(B) 1.00
(C) $0.80 \log$	(D) $0.90 \log$

SOL 1.59 The Correct option is (C).

Industrial substation of 4 MW load = P_L $Q_C = 2 \text{ MVAR}$ for load p.f. = 0.97 lagging If capacitor goes out of service than load p.f. = ? $\cos \phi = 0.97$ $\tan \phi = \tan(\cos^{-1}0.97) = 0.25$ $\frac{Q_L - Q_C}{P_L} = 0.25$ $\frac{Q_L - 2}{4} = 0.25 \Rightarrow Q_L = 3 \text{ MVAR}$ $\phi = \tan^{-1}\left(\frac{Q_L}{P_L}\right) = \tan^{-1}\left(\frac{3}{4}\right) = 36^\circ$ $\cos \phi = \cos 36^\circ = 0.8 \text{ lagging}$

MCQ 1.60 The network shown in the given figure has impedances in p.u. as indicated. The diagonal element Y_{22} of the bus admittance matrix Y_{BUS} of the network is



SOL 1.60 The Correct option is (D).

$$Y_{22} = ?$$

$$I_1 = V_1 Y_{11} + (V_1 - V_2) Y_{12}$$

$$= 0.05 V_1 - j10 (V_1 - V_2) = -j9.95 V_1 + j10 V_2$$

$$I_2 = (V_2 - V_1) Y_{21} + (V_2 - V_3) Y_{23}$$

$$= j10 V_1 - j9.9 V_2 - j0.1 V_3$$

$$Y_{22} = Y_{11} + Y_{23} + Y_2$$

$$= -j9.95 - j9.9 - 0.1j$$

$$= -j19.95$$

MCQ 1.61 A load centre is at an equidistant from the two thermal generating stations G_1 and G_2 as shown in the figure. The fuel cost characteristic of the generating stations are given by

$$F_1 = a + bP_1 + cP_1^2 \text{ Rs/hour}$$

 $F_2 = a + bP_2 + 2cP_2^2 \text{ Rs/ hour}$



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Where P_1 and P_2 are the generation in MW of G_1 and G_2 , respectively. For most

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economic generation to meet 300 MW of load P_1 and P_2 respectively, are (B) 100, 200 (A) 150, 150 (C) 200, 100 (D) 175, 125 **SOL 1.61** The Correct option is (C). $F_1 = a + bP_1 + cP_1^2$ Rs/hour $F_2 = a + bP_2 + 2cP_2^2$ Rs/hour For most economical operation $P_1 + P_2 = 300$ MW then $P_1, P_2 = ?$ We know for most economical operation $\frac{\partial F_1}{\partial P_1} = \frac{\partial F_2}{\partial P_2}$ $2cP_1 + b = 4cP_2 + b$ $P_1 = 2P_2$...(1) $P_1 + P_2 = 300$...(2) $P_1 = 200 \text{ MW}, P_2 = 100 \text{ MW}$ from eq (1) and (2)

MCQ 1.62 Two networks are connected in cascade as shown in the figure. With usual notations the equivalent A, B, C and D constants are obtained. Given that, $C = 0.025 \angle 45^\circ$, the value of Z_2 is

help $Z_1 = 10 \angle 30^\circ \Omega$ Z_2 (A) $10 \angle 30^{\circ} \Omega$ (B) $40\angle -45^\circ \Omega$ (C) 1Ω (D) 0Ω SOL 1.62 The Correct option is (B). We know that *ABCD* parameters $\begin{bmatrix} V_1 \\ I_1 \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} V_2 \\ I_1 \end{bmatrix}$ $B = \frac{V_1}{I_2}\Big|_{V=0}, \ C = \frac{I_1}{V_2}\Big|_{I=0}$ $C = \frac{\frac{V_1}{Z_1 + Z_2}}{\frac{V_1}{Z_1 + Z_2} \times Z_2} = \frac{1}{Z_2}$

 $Z_2 = \frac{1}{C}$

In figure

or

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$$=\frac{1}{0.025\angle 45^{\circ}}=40\angle -45^{\circ}$$

MCQ 1.63 A generator with constant 1.0 p.u. terminal voltage supplies power through a stepup transformer of 0.12 p.u. reactance and a double-circuit line to an infinite bus bar as shown in the figure. The infinite bus voltage is maintained at 1.0 p.u. Neglecting the resistances and suspectances of the system, the steady state stability power limit of the system is 6.25 p.u. If one of the double-circuit is tripped, then resulting steady state stability power limit in p.u. will be



SOL 1.64 The Correct option is (B).

(C) $Q \sin(8t + 60^{\circ})$

(D) $Q \sin(4t + 30^{\circ})$

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We can obtain the frequency ratio as following



 $\frac{f_Y}{f_X} = \frac{\text{meeting points of horizontal tangents}}{\text{meeting points of vertical tangents}}$ $\frac{f_Y}{f_X} = \frac{2}{4}$ $f_Y = \frac{1}{2}f_X$

There should exist a phase difference (15°) also to produce exact figure of-8.

- **MCQ 1.65** A DC ammeter has a resistance of 0.1 Ω and its current range is 0-100 A. If the range is to be extended to 0-500 A, then meter required the following shunt resistance
 - (A) 0.010 Ω (C) 0.025 Ω

IICIP

SOL 1.65 The Correct option is (C). The configuration is shown below



It is given that $I_m = 100$ A Range is to be extended to 0 - 500 A, I = 500 A

So,

$$I_m R_m = (I - I_m) R_{sh}$$

 $100 \times 0.1 = (500 - 100) R_{sh}$

$$R_{sh} = \frac{100 \times 0.1}{400}$$
$$= 0.025 \ \Omega$$

MCQ 1.66 The set-up in the figure is used to measure resistance R. The ammeter and voltmeter resistances are 0.01Ω and 2000Ω , respectively. Their readings are 2 A and 180

V, respectively, giving a measured resistances of 90 Ω The percentage error in the measurement is



= 4.71%

MCQ 1.67 A 1000 V DC supply has two 1-core cables as its positive and negative leads : their insulation resistances to earth are 4 M Ω and 6 M Ω , respectively, as shown in the figure. A voltmeter with resistance 50 k Ω is used to measure the insulation of the cable. When connected between the positive core and earth, then voltmeter reads

SOL 1.66



(C)
$$24 \text{ V}$$
 (D) 40

The Correct option is (A). The measurement system is shown below



- **MCQ 1.68** Two wattmeters, which are connected to measure the total power on a three-phase system supplying a balanced load, read 10.5 kW and -2.5 kW, respectively. The total power and the power factor, respectively, are
 - (A) 13.0 kW, 0.334 (B) 13.0 kW, 0.684 (C) 8.0 kW, 0.52 (D) 8.0 kW, 0.334
- **SOL 1.68** The Correct option is (D).

Total power
$$P = P_1 + P_2$$

= 10.5 - 2.5
= 8 kW

Power factor $= \cos \theta$

Where

$$\theta = \tan^{-1} \left[\sqrt{3} \left(\frac{P_2 - P_1}{P_2 + P_1} \right) \right]$$
$$= \tan^{-1} \left[\sqrt{3} \times \frac{-13}{8} \right]$$
$$= -70.43^{\circ}$$

Power factor $= \cos \theta = 0.334$

MCQ 1.69 The common emitter amplifier shown in the figure is biased using a 1 mA ideal current source. The approximate base current value is



SOL 1.69 The Correct option is (B). Since the transistor is operating in active region. $I_E \approx \beta I_B$

$$I_{B} = \frac{I_{E}}{\beta} \mathbf{a} \mathbf{a} \mathbf{a} \mathbf{b} \mathbf{a}$$
$$= \frac{1 \text{ mA}}{100} = 10 \ \mu \text{A}$$

MCQ 1.70 Consider the inverting amplifier, using an ideal operational amplifier shown in the figure. The designer wishes to realize the input resistance seen by the small-signal source to be as large as possible, while keeping the voltage gain between -10 and -25. The upper limit on R_F is 1 M Ω . The value of R_1 should be



(A) Infinity	(B) $1 M\Omega$
(C) 100 k Ω	(D) 40 k Ω

SOL 1.70 The Correct option is (C). Gain of the inverting amplifier is given by,

$$A_v = -\frac{R_F}{R_1}$$

$$A_v = -\frac{1 \times 10^6}{R_1}, \qquad \qquad R_F = 1 \quad M\Omega$$

$$R_1 = -\frac{1 \times 10^6}{A_v} \qquad \qquad A_v = -10 \text{ to } -25 \text{ so value of } R_1$$

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$$R_{1} = \frac{10^{6}}{10} = 100 \text{ k}\Omega \qquad \text{for } A_{v} = -10$$
$$R_{1}^{'} = \frac{10^{6}}{25} = 40 \text{ k}\Omega \qquad \text{for } A_{v} = -25$$

 R_1 should be as large as possible so $R_1 = 100 \text{ k}\Omega$

MCQ 1.71 The typical frequency response of a two-stage direct coupled voltage amplifier is as shown in figure



- **SOL 1.71** The Correct option is (B). Direct coupled amplifiers or DC-coupled amplifiers provides gain at dc or very low frequency also.
- **MCQ 1.72** In the given figure, if the input is a sinusoidal signal, the output will appear as shown





SOL 1.72 The Correct option is (C). Since there is no feedback in the circuit and ideally op-amp has a very high value of open loop gain, so it goes into saturation (ouput is either + V or - V) for small values of input.

The input is applied to negative terminal of op-amp, so in positive half cycle it saturates to -V and in negative half cycle it goes to +V.

MCQ 1.73 Select the circuit which will produce the given output Q for the input signals X_1 and X_2 given in the figure



SOL 1.73

From the given input output waveforms truth table for the circuit is drawn as

 $\begin{array}{ccccccc} X_1 & X_2 & Q \\ 1 & 0 & 1 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \\ \vdots & (A) & \zeta & V \end{array}$

In option (A), for $X_1 = 1, Q = 0$ so it is eliminated. In option (C), for $X_1 = 0, Q = 0$ (always), so it is also eliminated.

(check)

In option (D), for $X_1 = 0, Q = 1$, which does not match the truth table. Only option (B) satisfies the truth table. Hence (B) is correct option.

MCQ 1.74 If X_1 and X_2 are the inputs to the circuit shown in the figure, the output Q is



(A) $\overline{X_1 + X_2}$ (C) $\overline{X_1} \cdot X_2$

(B)
$$X_1 \bullet X_2$$

(D) $X_1 \bullet \overline{X_2}$

SOL 1.74 The Correct option is (D). In the given circuit NMOS Q_1 and Q_3 makes an inverter circuit. Q_4 and Q_5 are in parallel works as an OR circuit and Q_5 is an output inverter. So output is

$$Q = \overline{X_1} + \overline{X_2} = X_1 \cdot \overline{X_2}$$

MCQ 1.75 In the figure, as long as $X_1 = 1$ and $X_2 = 1$, the output Q remains



- (A) at 1(B) at 0(C) at its initial value(D) unstable
- **SOL 1.75** The Correct option is (D). Let Q(t) is the present state then from the circuit,



So, the next state is given by $Q(t+1) = \overline{Q}(t)$ (unstable)

MCQ 1.76 The figure shows the voltage across a power semiconductor device and the current

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through the device during a switching transitions. If the transition a turn ON transition or a turn OFF transition ? What is the energy lost during the transition?

(A) Turn ON, $\frac{VI}{2}(t_1 + t_2)$ (B) Turn OFF, $VI(t_1 + t_2)$ (D) Turn OFF, $\frac{VI}{2}(t_1 + t_2)$ (C) Turn ON, $VI(t_1 + t_2)$ **SOL 1.76** The Correct option is (A). In Ideal condition we take voltage across the device is zero. average power loss during switching $=\frac{VI}{2}(t_1+t_2)$ (turn ON) An electronics switch S is required to block voltage of either polarity during its **MCQ 1.77** OFF state as shown in the figure (a). This switch is required to conduct in only one direction its ON state as shown in the figure (b) 1 fig (b) Which of the following are valid realizations of the switch S? P. 1-1' Q. 1-S. 1— R. 1 1' (A) Only P (B) P and Q

(C) P and R

(D) R and S

So in P thyristor blocks voltage in both polarities until gate is triggered and also in R transistor along with diode can do same process.

MCQ 1.78 The given figure shows a step-down chopper switched at 1 kHz with a duty ratio D = 0.5. The peak-peak ripple in the load current is close to



(C) 4 kg-m² (D) 4 Nm²

SOL 1.79 The Correct option is (C). $T_{\rm st} = 15 \text{ Nm}$

$$T_{
m st} = 15~
m Nm$$

 $T_L = 7~
m Nm$
 $lpha = 2~
m rad/
m sec^2$
 $T = Ilpha$
 $T = T_{
m st} - T_L = 8~
m Nm$
 $I = rac{8}{2} = 4~
m kgm^2$

 \mathbf{SO}

MCQ 1.80 Consider a phase-controlled converter shown in the figure. The thyristor is fired at an angle α in every positive half cycle of the input voltage. If the peak value of the instantaneous output voltage equals 230 V, the firing angle α is close to



Linked Answer Questions : Q.81 to Q.90 Carry Two Marks Each

Statement for Linked Answer Questions 81 and 82

A coil of inductance 10 H and resistance 40 Ω is connected as shown in the figure. After the switch S has been in contact with point 1 for a very long time, it is moved to point 2 at, t = 0.

MCQ 1.81 If, at $t = 0^+$, the voltage across the coil is 120 V, the value of resistance R is



SOL 1.81

When the switch is at position 1, current in inductor is given as



At t = 0, when switch is moved to position 1,inductor current does not change simultaneously so



Hence (A) is correct option.

MCQ 1.82 For the value as obtained in (a), the time taken for 95% of the stored energy to be dissipated is close to

(A) $0.10 \sec$	(B) 0.15 sec
(C) $0.50 \sec$	(D) $1.0 \sec$

SOL 1.82 Let stored energy and dissipated energy are E_1 and E_2 respectively. Then Current

$$\frac{i_2^2}{i_1^2} = \frac{E_2}{E_1} = 0.95$$
$$i_2 = \sqrt{0.95} i_1 = 0.97 i_1$$

Current at any time t, when the switch is in position (2) is given by

 $i(t) = i_1 e^{-\frac{R}{L}t} = 2e^{-\frac{60}{10}t} = 2e^{-6t}$

After 95% of energy dissipated current remaining in the circuit is

$$i = 2 - 2 \times 0.97 = 0.05$$
 A
 $0.05 = 2e^{-6t}$

So,

 $t \approx 0.50 \, \mathrm{sec}$

Hence (C) is correct option.

Statement for Linked Answer Questions 83 and 84

A state variable system $\dot{\mathbf{X}}(t) = \begin{bmatrix} 0 & 1 \\ 0 & -3 \end{bmatrix} \mathbf{X}(t) + \begin{bmatrix} 1 \\ 0 \end{bmatrix} \mathbf{u}(t)$ with the initial condition $\boldsymbol{X}(0) = [-1, 3]^T$ and the unit step input u(t) has **MCQ 1.83** The state transition matrix (A) $\begin{bmatrix} 1 & \frac{1}{3}(1-e^{-3t}) \\ 0 & e^{-3t} \end{bmatrix}$ (B) $\begin{vmatrix} 1 & \frac{1}{3}(e^{-t} - e^{-3t}) \\ 0 & e^{-t} \end{vmatrix}$ (C) $\begin{bmatrix} 1 & \frac{1}{3}(e^{3-t} - e^{-3t}) \\ 0 & e^{-3t} \end{bmatrix}$ (D) $\begin{bmatrix} 1 & (1 - e^{-t}) \\ 0 & e^{-t} \end{bmatrix}$ Given state equation **SOL 1.83** $\dot{\boldsymbol{X}}(t) = \begin{bmatrix} 0 & 1 \\ 0 & -3 \end{bmatrix} \boldsymbol{X}(t) + \begin{bmatrix} 1 \\ 0 \end{bmatrix} \boldsymbol{u}(t)$ Here $A = \begin{bmatrix} 0 & 1 \\ 0 & -3 \end{bmatrix}, B = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$ State transition matrix is given by, $\Phi(t) = \mathcal{L}^{-1}[(sI - A)^{-1}]$ $[sI - A] = \begin{bmatrix} s & 0 \\ 0 & s \end{bmatrix} - \begin{bmatrix} 0 & 0 \\ 0 & 3 \end{bmatrix} = \begin{bmatrix} s & -1 \\ 0 & s + 3 \end{bmatrix}$ $[sI - A]^{-1} = \frac{1}{s(s+3)} \begin{bmatrix} s+3 & 1\\ 0 & s \end{bmatrix}$ $= \begin{vmatrix} \frac{1}{s} & \frac{1}{s(s+3)} \\ 0 & \frac{1}{(s+3)} \end{vmatrix}$ $\Phi(t) = \mathcal{L}^{-1}[(sI - A)^{-1}]$ $= \begin{vmatrix} 1 & \frac{1}{3} (1 - e^{-3t}) \\ 0 & e^{-3t} \end{vmatrix}$ Hence (A) is correct option.

MCQ 1.84 The state transition equation
(A)
$$\mathbf{X}(t) = \begin{bmatrix} t - e^{-t} \\ e^{-t} \end{bmatrix}$$
(B) $\mathbf{X}(t) = \begin{bmatrix} 1 - e^{-t} \\ 3e^{-3t} \end{bmatrix}$
(C) $\mathbf{X}(t) = \begin{bmatrix} t - e^{3t} \\ 3e^{-3t} \end{bmatrix}$
(D) $\mathbf{X}(t) = \begin{bmatrix} t - e^{-3} \\ e^{-t} \end{bmatrix}$

SOL 1.84

State transition equation is given by $\boldsymbol{X}(s) = \boldsymbol{\Phi}(s) \, \boldsymbol{X}(0) + \boldsymbol{\Phi}(s) \, B \, \boldsymbol{U}(s)$

(B)
$$\boldsymbol{X}(t) = \begin{bmatrix} 1 - e^{-t} \\ 3e^{-3t} \end{bmatrix}$$

(D) $\boldsymbol{X}(t) = \begin{bmatrix} t - e^{-3t} \\ e^{-t} \end{bmatrix}$

Here $\Phi(s) \rightarrow$ state transition matrix $\Phi(s) = \begin{bmatrix} \frac{1}{s} & \frac{1}{s(s+3)} \\ 0 & \frac{1}{(s+3)} \end{bmatrix}$ $X(0) \rightarrow$ initial condition $X(0) = \begin{bmatrix} -1 \\ 3 \end{bmatrix}$ $B = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$ $B = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$ So $X(s) = \begin{bmatrix} \frac{1}{s} & \frac{1}{s(s+3)} \\ 0 & \frac{1}{(s+3)} \end{bmatrix} \begin{bmatrix} -1 \\ 3 \end{bmatrix} + \begin{bmatrix} \frac{1}{s} & \frac{1}{(s+3)s} \\ 0 & \frac{1}{s+3} \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} \frac{1}{s}$ $= \begin{bmatrix} -\frac{1}{s} + \frac{3}{s(s+3)} \\ 0 + \frac{3}{s+3} \end{bmatrix} + \begin{bmatrix} \frac{1}{s} \end{bmatrix} \frac{1}{s}$ $= \begin{bmatrix} -\frac{1}{s} + \frac{3}{s(s+3)} \\ 0 + \frac{3}{s+3} \end{bmatrix} + \begin{bmatrix} \frac{1}{s^2} \\ 0 \end{bmatrix} \frac{1}{s}$ $= \begin{bmatrix} -\frac{1}{s+3} \\ \frac{3}{s+3} \end{bmatrix} + \begin{bmatrix} \frac{1}{s^2} \\ 0 \end{bmatrix} \frac{1}{s}$ $X(s) = \begin{bmatrix} \frac{1}{s^2} - \frac{1}{s+3} \\ \frac{3}{s+3} \end{bmatrix}$

Taking inverse Laplace transform, we get state transition equation as,

$$\boldsymbol{X}(t) = \begin{bmatrix} t - e^{-3t} \\ 3e^{-3t} \end{bmatrix}$$

Hence (C) is correct option.

Statement for Linked Answer Questions 85 and 86

A 1000 kVA, 6.6 kV, 3-phase star connected cylindrical pole synchronous generator has a synchronous reactance of 20 Ω . Neglect the armature resistance and consider operation at full load and unity power factor.

MCQ 1.85	The induced emf(line-to-line) is close to	
	(A) 5.5 kV	(B) 7.26 kV
	(C) 9.6 kV	(D) 12.5 kV

SOL 1.85 Given

P = 1000 kVA, 6.6 kV

Reactance = 20 Ω and neglecting the armature resistance at full load and unity

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power factor
So

$$P = \sqrt{3} V_{r} I_{r}$$

$$I = \frac{1000}{\sqrt{3 \times 6.6}} = 87.47 \text{ A}$$

$$\overbrace{L}^{E_{gh}} = \overbrace{\left(\frac{6.5}{\sqrt{3}}\right)^{2}}^{L_{s}}$$
So,

$$IX = 87.47 \times 20 = 1.75 \text{ kV}$$

$$\overbrace{E_{gh}}^{L_{s}} = \left(\frac{6.5}{\sqrt{3}}\right)^{2} + (1.75)^{2}$$

$$E_{ph} = \left(\sqrt{\left(\frac{6.5}{\sqrt{3}}\right)^{2}} + (1.75)^{2}\right)$$

$$E_{r} = \sqrt{3} E_{ph}$$

$$E_{L} = 1.732 \times 42$$

$$E_{L} = 7.26 \text{ kV}$$
Hence (B) is correct option.
MCQ 1.86 The power(or torque) angle is close to
(A) 13.9^{*}
(C) 24.6[°]
(D) 33.0[°]
Sol 1.86 Hence (C) is correct option.
Torque angle $\alpha_{x} = \tan^{-1}\left(\frac{X_{3}}{R_{y}}\right)$

$$\overbrace{L}^{T} = \frac{1}{\sqrt{6.6} \text{ kV}}$$

$$\alpha_{x} = \tan^{-1}\left(\frac{\sqrt{3} \times 1.75}{6.6}\right)$$

 $\alpha_z = 24.6^{\circ}$

Statement for Linked Answer Questions 87 and 88

At a 220 kV substation of a power system, it is given that the three-phase fault level is 4000 MVA and single-line to ground fault level is 5000 MVA Neglecting the resistance and the shunt suspectances of the system.

MCQ 1.87The positive sequence driving point reactance at the bus is
(A) 2.5 Ω (B) 4.033 Ω

(C	15.5Ω (1	D)	12.1	Ω
\				

SOL 1.87 Given data

Substation Level = 220 kV3- ϕ fault level = 4000 MVALG fault level = 5000 MVA

Positive sequence reactance:



- MCQ 1.88The zero sequence driving point reactance at the bus is
(A) 2.2 Ω (B) 4.84 Ω
(C) 18.18 Ω (D) 22.72 Ω
- **SOL 1.88** Zero sequence Reactance $X_0 = ?$

$$I_{f} = \frac{5000}{\sqrt{3} \times 220}$$

$$I_{a1} = I_{a2} = I_{a0} = \frac{I_{f}}{\frac{220}{3\sqrt{3} \times 220}}$$

$$X_{1} + X_{2} + X_{0} = \frac{V_{ph}}{I_{a1}} = \frac{\frac{220}{\sqrt{3}}}{\frac{5000}{220 \times 3\sqrt{3}}}$$

$$X_{1} + X_{2} + X_{0} = \frac{220 \times 220}{3 \times 5000} = 29.04 \Omega$$

$$X_{1} = X_{2} = 12.1 \Omega$$

$$X_{0} = 29.04 - 12.1 - 12.1$$

$$= 4.84 \Omega$$

Hence (B) is correct option.

Statement for Linked Answer Questions 89 and 90

Assume that the threshold voltage of the N-channel MOSFET shown in figure is + 0.75 V. The output characteristics of the MOSFET are also shown



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$$A_v = \frac{v_o}{v_i} = -g_m R_D$$
$$= -(1 \text{ mS}) (10 \text{ k}\Omega)$$
$$= -10$$

Hence (D) is correct option.

	Answer Sheet								
1.	(C)	19.	(B)	37.	(C)	55.	(B)	73.	(B)
2.	(A)	20.	(A)	38.	(C)	56.	(B)	74.	(D)
3.	(D)	21.	(C)	39.	(B)	57.	(A)	75.	(D)
4.	(B)	22.	(A)	40.	(C)	58.	(D)	76.	(A)
5.	(D)	23.	(A)	41.	(D)	59.	(C)	77.	(C)
6.	(C)	24.	(C)	42.	(B)	60.	(D)	78.	(C)
7.	(A)	25.	(D)	43.	(B)	61.	(C)	79.	(C)
8.	(A)	26.	(C)	44.	(A)	62.	(B)	80.	(B)
9.	(D)	27.	(B)	45.	l _(C) g	63.	(D)	81.	(A)
10.	(D)	28.	(A)	46.	(B)	64.	(B)	82.	(C)
11.	(C)	29.	(B)	47.	(A) G	65.	(C)	83.	(A)
12.	(A)	30.	(C)	48.	(D)	66.	(D)	84.	(C)
13.	(D)	31.	(C)	49.	(B)	67.	(A)	85.	(B)
14.	(B)	32.	(A)	50.	(A)	68.	(D)	86.	(C)
15.	(A)	33.	(A)	51.	(B)	69.	(B)	87.	(D)
16.	(B)	34.	(C)	52.	(D)	70.	(C)	88.	(B)
17.	(D)	35.	(A)	53.	(C)	71.	(B)	89.	(B)
18.	(D)	36.	(A)	54.	(*)	72.	(C)	90.	(D)

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